

PROGRESSION THROUGH CALCULATIONS FOR MULTIPLICATION

MENTAL CALCULATIONS

(ongoing)

These are a **selection** of mental calculation strategies:

Doubling and halving

Applying the knowledge of doubles and halves to known facts.

e.g. 8×4 is double 4×4

Using multiplication facts

Tables should be taught everyday from Y1 onwards, either as part of the mental oral starter or other times as appropriate within the day.

Year 1	2 times table 5 times table 10 times table	Counting in
Year 2	2 times table 3 times table 5 times table 10 times table	Counting in 3s. Recall of 2s, 5s & 10s.
Year 3	2 times table 3 times table 4 times table 5 times table 6 times table 8 times table 10 times table	Counting in 4s, 8s, 50s & 100s. Recall of 3s, 4s & 8s.
Year 4	Counting in 6s, 7s, 9s, 25s, 1000s. Derive and recall all multiplication facts up to 12×12	

Using and applying division facts

Children should be able to utilise their tables knowledge to derive other facts.

e.g. If I know $3 \times 7 = 21$, what else do I know?

$30 \times 7 = 210$, $300 \times 7 = 2100$, $3000 \times 7 = 21\ 000$, $0.3 \times 7 = 2.1$ etc

Use closely related facts already known

$$\begin{aligned} 13 \times 11 &= (13 \times 10) + (13 \times 1) \\ &= 130 + 13 \\ &= 143 \end{aligned}$$

Multiplying by 10 or 100

Knowing that the effect of multiplying by 10 is a shift in the digits one place to the left.

Knowing that the effect of multiplying by 100 is a shift in the digits two places to the left.

Partitioning

$$23 \times 4 = (20 \times 4) + (3 \times 4)$$

$$= 80 + 12$$

$$= 102$$

Use of factors

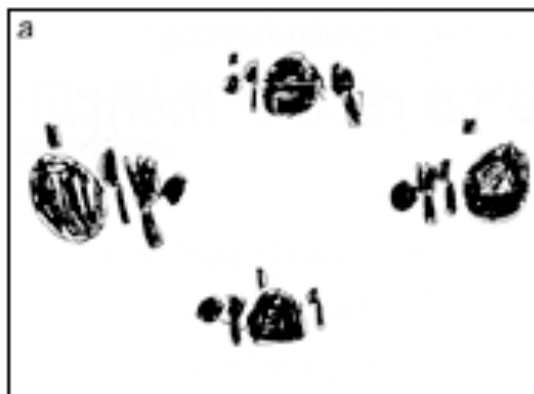
$$8 \times 12 = 8 \times 4 \times 3$$

MANY MENTAL CALCULATION STRATEGIES WILL CONTINUE TO BE USED. THEY ARE NOT REPLACED BY WRITTEN METHODS.

THE FOLLOWING ARE STANDARDS THAT WE EXPECT THE MAJORITY OF CHILDREN TO ACHIEVE.

YR and Y1

Children will experience equal groups of objects and will count in 2s, 5s and 10s. They will work on practical problem solving activities involving equal sets or groups.



Y1

Children will develop an understanding of multiplication by using arrays for the 2, 5 and 10 times tables e.g. $5 \times 2 = 10$



Y2

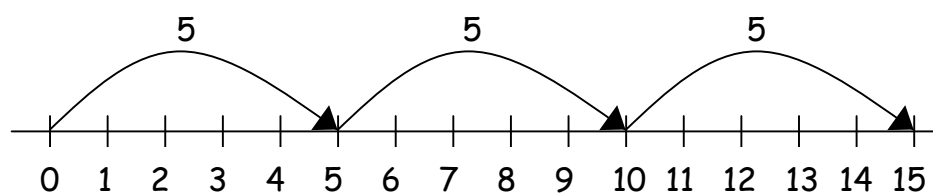
Children will develop their understanding of multiplication and use jottings to support calculation:

✓ Repeated addition

3 times 5 is $5 + 5 + 5 = 15$ or 3 lots of 5 or 5×3

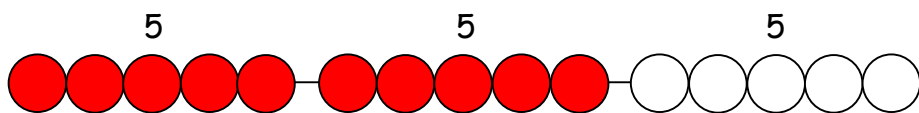
Repeated addition can be shown easily on a number line:

$$5 \times 3 = 5 + 5 + 5$$



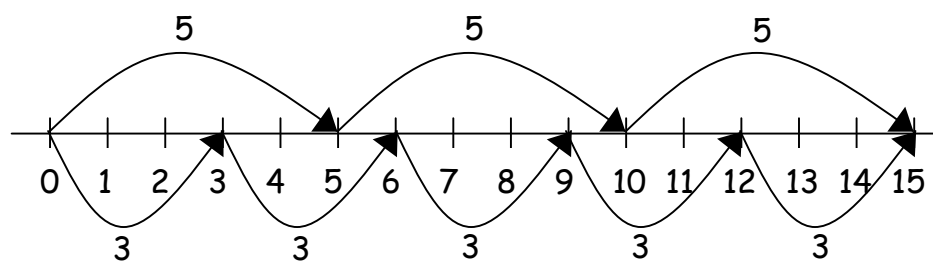
and on a bead bar:

$$5 \times 3 = 5 + 5 + 5$$



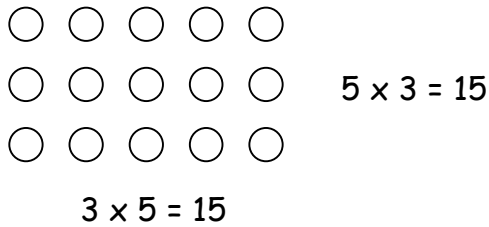
✓ Commutativity

Children should know that 3×5 has the same answer as 5×3 . This can also be shown on the number line.



✓ **Arrays**

Children should be able to model a multiplication calculation using an array. This knowledge will support with the development of the grid method.



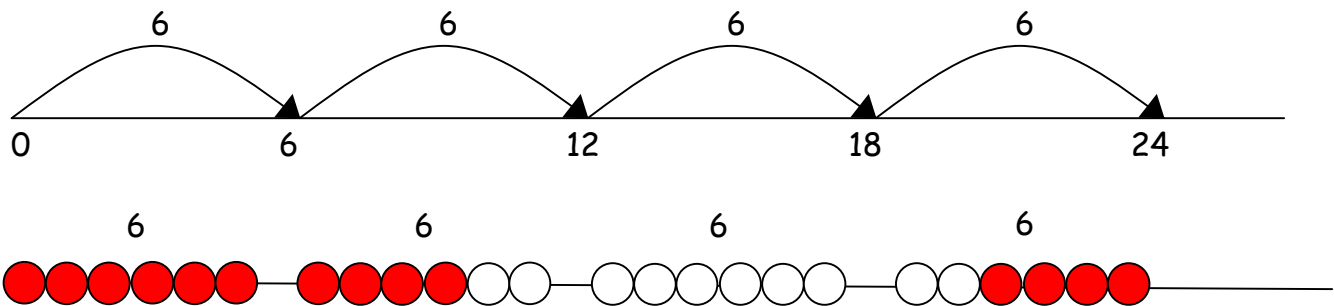
Y3

Children will continue to use:

✓ **Repeated addition**

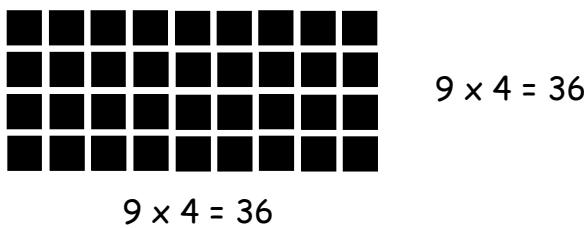
4 times 6 is $6 + 6 + 6 + 6 = 24$ or 4 lots of 6 or 6×4

Children should use number lines or bead bars to support their understanding.



✓ **Arrays**

Children should be able to model a multiplication calculation using an array. This knowledge will support with the development of the grid method.



Children will also develop an understanding of

✓ **Scaling**

e.g. Find a ribbon that is 4 times as long as the blue ribbon



✓ **Using symbols to stand for unknown numbers to complete equations using inverse operations**

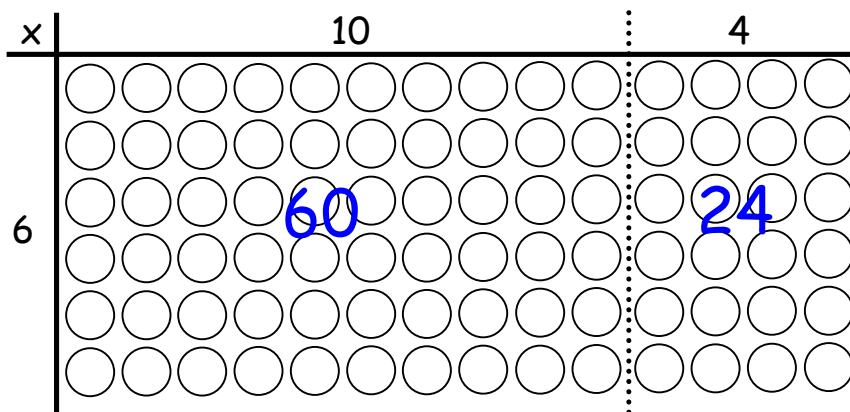
$\square \times 5 = 20$ $3 \times \triangle = 18$ $\square \times \circ = 32$

✓ **Partitioning**

$$\begin{aligned} 38 \times 5 &= (30 \times 5) + (8 \times 5) \\ &= 150 + 40 \\ &= 190 \end{aligned}$$

✓ **Arrays leading to grid method**

Children will continue to use arrays where appropriate leading into the grid method of multiplication.



$$\begin{aligned} &(6 \times 10) + (6 \times 4) \\ &60 + 24 \\ &84 \end{aligned}$$

Grid method

TU x U

(Short multiplication - multiplication by a single digit)

23×8

Children will approximate first
 23×8 is approximately $25 \times 8 = 200$

$$\begin{array}{r}
 \times \quad 20 \quad 3 \\
 8 \quad \boxed{160} \quad \boxed{24} \\
 \hline
 160 \\
 + \quad 24 \\
 \hline
 184
 \end{array}$$

Y4

Grid method

TU × U

(Short multiplication - multiplication by a single digit)

$$23 \times 8$$

Children will approximate first

23×8 is approximately $25 \times 8 = 200$

$$\begin{array}{r}
 \times \quad 20 \quad 3 \\
 8 \quad \boxed{160} \quad \boxed{24} \\
 \hline
 160 \\
 + \quad 24 \\
 \hline
 184
 \end{array}$$

Grid method

HTU × U

(Short multiplication - multiplication by a single digit)

$$346 \times 9$$

Children will approximate first

346×9 is approximately $350 \times 10 = 3500$

$$\begin{array}{r} \times \quad 300 \quad 40 \quad 6 \\ 9 \quad \boxed{2700} \quad \boxed{360} \quad \boxed{54} \end{array}$$

$$\begin{array}{r} 2700 \\ + 360 \\ + \quad 54 \\ \hline 3114 \\ \small{11} \end{array}$$

Expanded vertical short multiplication

TU × U

(Short multiplication - multiplication by a single digit)

23×8 Starting with most significant digits, moving onto to least significant digits (see HTU × U)

Children will approximate first

23×8 is approximately $25 \times 8 = 200$

$$\begin{array}{r} \quad 23 \\ X \quad \underline{8} \\ 160 \quad (8 \times 20) \\ \underline{24} \quad (8 \times 3) \\ 184 \end{array}$$

HTU × U

(Short multiplication - multiplication by a single digit)

$$\begin{array}{r} \quad 346 \\ X \quad \underline{9} \\ 54 \quad (9 \times 6) \\ 360 \quad (9 \times 40) \\ \underline{2700} \quad (9 \times 300) \\ 3114 \end{array}$$

Y5

Grid method

HTU x U

(Short multiplication - multiplication by a single digit)

$$346 \times 9$$

Children will approximate first

$$346 \times 9 \text{ is approximately } 350 \times 10 = 3500$$

x	300	40	6	
9	2700	360	54	2700
				+ 360
				+ <u>54</u>
				<u>3114</u>
				1 1

TU x TU

(Long multiplication - multiplication by more than a single digit)

$$72 \times 38$$

Children will approximate first

$$72 \times 38 \text{ is approximately } 70 \times 40 = 2800$$

x	70	2	
30	2100	60	2100
8	560	16	+ 560
			+ 60
			+ <u>16</u>
			<u>2736</u>
			1

Using similar methods, they will be able to multiply HTU x TU & ThHTU x U.

Using similar methods, they will be able to multiply decimals with one decimal place by a single digit number, approximating first. They should know that the decimal points line up under each other.

e.g. 4.9×3

Children will approximate first

4.9×3 is approximately $5 \times 3 = 15$

$$\begin{array}{r}
 \times \quad 4 \quad 0.9 \\
 3 \quad \boxed{12} \quad \boxed{2.7} \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 12 \\
 + \quad 2.7 \\
 \hline
 14.7 \\
 \hline
 \end{array}$$

Short multiplication

HTU \times U

(Short multiplication - multiplication by a single digit)

346×9

Children will approximate first

346×9 is approximately $350 \times 10 = 3500$

$$\begin{array}{r}
 346 \\
 \times \quad \underline{9} \\
 \hline
 3114 \\
 \hline
 \end{array}$$

Using similar methods, they will be able to multiply ThHTU \times U.

Long multiplication

(Long multiplication - multiplication by more than a single digit)

$$372 \times 24$$

Children will approximate first

372×24 is approximately $400 \times 25 = 10000$

$$\begin{array}{r} 372 \\ \times 24 \\ \hline 1488 \\ 2 \\ \hline 7440 \\ 1 \\ \hline 8928 \\ 1 \end{array}$$

Y6

ThHTU \times U

(Short multiplication - multiplication by a single digit)

$$4346 \times 8$$

Children will approximate first

4346×8 is approximately $4346 \times 10 = 43460$

$$\begin{array}{r} 4346 \\ \times 8 \\ \hline 34768 \\ 2 \ 3 \ 4 \end{array}$$

HTU \times TU

(Long multiplication - multiplication by more than a single digit)

$$372 \times 24$$

Children will approximate first

372×24 is approximately $400 \times 25 = 10000$

$$\begin{array}{r}
 372 \\
 \times \quad 24 \\
 \hline
 1488 \\
 ^2 \\
 7440 \\
 \hline
 8928 \\
 ^1
 \end{array}$$

Using similar methods, they will be able to multiply ThHTU x TU.

Using similar methods, they will be able to multiply decimals with up to two decimal places by a single digit number and then two digit numbers, approximating first. They should know that the decimal points line up under each other.

For example:

$$4.92 \times 3$$

Children will approximate first

$$4.92 \times 3 \text{ is approximately } 5 \times 3 = 15$$

$$\begin{array}{r}
 4.92 \\
 \times \quad 3 \\
 \hline
 14.76 \\
 ^2
 \end{array}$$

+ - + - + - + - + - + - +

By the end of year 6, children will have a range of calculation methods, mental and written. Selection will depend upon the numbers involved.

Children should not be made to go onto the next stage if:

- 1) they are not ready.
- 2) they are not confident.

Children should be encouraged to approximate their answers before calculating.

Children should be encouraged to consider if a mental calculation would be appropriate before using written methods.